

# Two-Color Laser Induced Electron Emission from Biased Metal Surface

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**Abstract:** By solving the time-dependent Schrödinger equation, we construct an exact analytical solution for nonlinear ultrafast electron emission from a dc-biased metal surface illuminated by two-color laser fields. Our results show a large dc bias can significantly increase the photoemission current, while maintaining a strong current modulation with respect to the phase delay of the two-color lasers. Application of our model to time-resolved photoelectron spectroscopy shows the dynamics of  $n$ -photon excited states depends strongly on the dc field.

**Keywords:** ultrafast photoemission; field emission; two-color lasers; analytical solution; current modulation depth.

## Introduction

Electron emission from nanostructures, as driven by high-intensity lasers, is a robust method to control electron dynamics in ultrafast scales. It is important to the development of time-resolved electron microscopes, tabletop particle accelerators, free electron lasers, and nanoscale vacuum electronics [1-3]. Recently, photoelectron emission from nanotips driven by two-color lasers has aroused intense interests [4-6], because of the relatively straightforward manipulation of two-color waveform and the substantial emission current modulation depth. However, the role of dc bias on two-color photoemission processes is not well studied. In this work, we present an exact analytical solution for nonlinear ultrafast photoemission from a dc-biased metal surface driven by two-color laser fields, by the solving time-dependent Schrödinger equation (TDSE) exactly [6-8]. Combined effects of a dc electric field and two-color laser fields are systematically analyzed.

Our one-dimensional (1D) model (see Fig. 1) considers electrons with initial energy  $\varepsilon$  emitted from a metal surface at  $x = 0$  under a dc electric field  $F_0$  and the illumination of two-color laser fields  $F_1 \cos(\omega t)$  and  $F_2 \cos(\beta \omega t + \theta)$ , where  $F_1$  and  $F_2$  are the amplitudes of laser fields,  $\omega$  is the fundamental laser frequency,  $\beta$  is a positive integer, and  $\theta$  is the relative phase [8]. The potential energy can be written as  $\Phi(x, t) = 0$  for  $x < 0$  inside the metal, and  $\Phi(x, t) = W + E_F - exF_0 - exF_1 \cos(\omega t) - exF_2 \cos(\beta \omega t + \theta)$  for  $x > 0$  in the vacuum, where  $E_F$  and  $W$  are the metal Fermi energy and work function respectively. By solving TDSE,

$$i\hbar \frac{\partial \psi(x, t)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi(x, t)}{\partial x^2} + \Phi(x, t) \psi(x, t), \quad (1)$$

the exact solution of electron wave function  $\psi(x, t)$  for  $x < 0$  and  $x > 0$  is obtained [8], which denotes the superposition of a set of electron waves with eigenenergies  $\varepsilon + n\hbar\omega$ . By applying boundary conditions that both  $\psi(x, t)$  and  $\partial\psi(x, t)/\partial x$  are continuous at  $x = 0$ , the amplitude of wave function at each state

can be determined. Following the probability current density  $J(x, t) = (i\hbar/2m)(\psi\nabla\psi^* - \psi^*\nabla\psi)$ , the normalized emission current density, defined as the ratio of the transmitted current density over the incident current density,  $w(\varepsilon, x, t) = J_t(\varepsilon, x, t)/J_i(\varepsilon, x, t)$ , is calculated.

Photoelectron energy spectra for different in-phase ( $\theta=0$ ) two-color  $\omega$ -laser  $F_1$  and  $2\omega$ -laser  $F_2$ , and dc fields  $F_0$  are shown in Fig. 2 [8]. The default values for the calculations are  $E_F = 5.53$  eV,  $W = 5.1$  eV (gold);  $\hbar\omega = 1.55$  eV ( $\lambda = 800$  nm). When  $F_0$  is turned off (Fig. 2(a)), the dominant emission process is four-photon absorption ( $n = 4$ ) for the  $\omega$ -laser  $F_1$ , indicating electrons at the Fermi level need to absorb at least four photons to overcome the potential barrier ( $W/\hbar\omega = 3.29$ ). Applying a strong dc field  $F_0$  opens more tunneling emission channels ( $n < 4$ ) as shown in Fig. 2(b). For a fixed  $F_0$ , the energy spectra become broader as  $F_1$  increases, because higher order  $n$ -photon processes contribute to the photoemission.

Figure 3 shows the combined effects of the dc field  $F_0$  and the interference between two-color lasers on the total emission current density  $\langle w \rangle$  and modulation depth  $\Gamma$ . As shown in Fig. 3(a),  $\langle w \rangle$  oscillates as a function of  $\theta$  with a period of  $2\pi$ , and the maximum (minimum) values of  $\langle w \rangle$  occur around  $\theta=0$  ( $\pi$ ) for a given  $F_0$ . The modulation depth,  $\Gamma = (\langle w \rangle_{max} - \langle w \rangle_{min}) / (\langle w \rangle_{max} + \langle w \rangle_{min})$ , as a function of  $F_0$  is shown in Fig. 3(b). As  $F_0$  increases,  $\Gamma$  decreases. However, for  $F_0$  up to 3 V/nm ( $\gg$  the laser fields  $F_1 = 1.6$  V/nm and  $F_2 = 0.22$  V/nm), strong emission current modulation still persists ( $\Gamma \geq 70\%$ ), with significantly increased total photoemission current. This suggests a practical way to maintain an intense modulation to high-current photoemission, by simply adding a strong dc bias and a weak harmonic laser [8].

Application of our model to the time-resolved photoelectron spectroscopy of a tungsten nanotip is shown in Fig. 4. When the dc field is small,  $F_0 = 0.01$  V/nm,  $n$ -photon excited states are modulated in the same way as a function of the phase delay  $\theta$ . However, when  $F_0 = 0.09$  V/nm, the excited states behave differently with respect to  $\theta$ . This demonstrates the dynamics of  $n$ -photon excited states due to two-color lasers depends strongly on the dc bias.

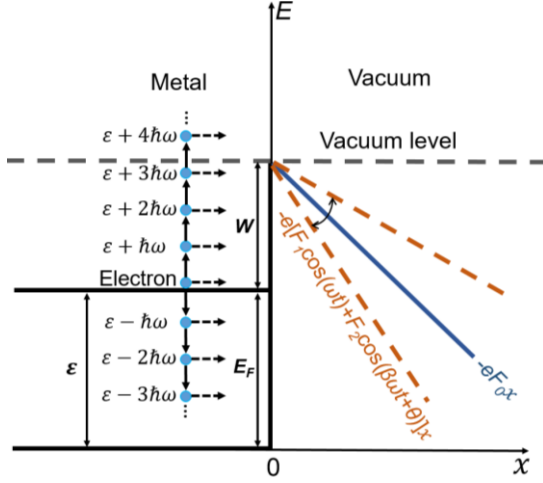
## Acknowledgements

This work is supported by the Air Force Office of Science Research (AFOSR) YIP Award No. FA9550-18-1-0061.

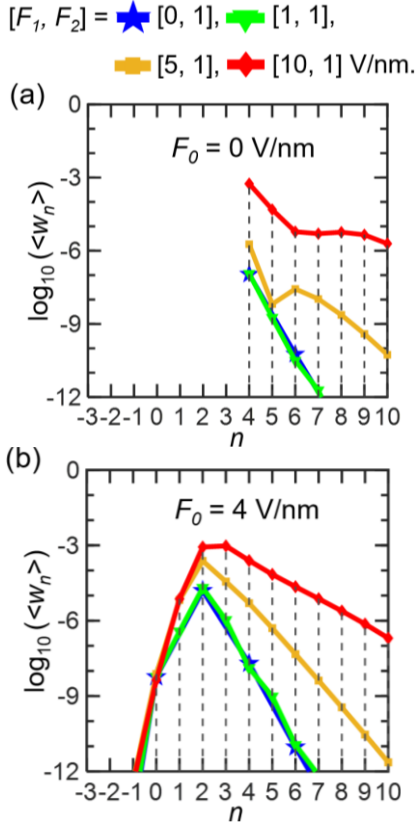
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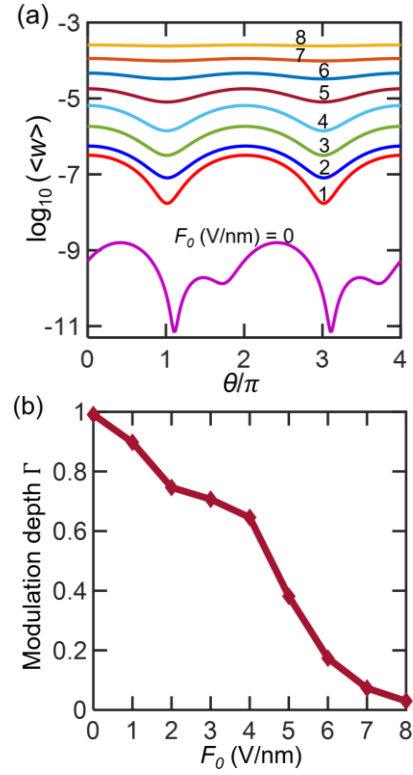
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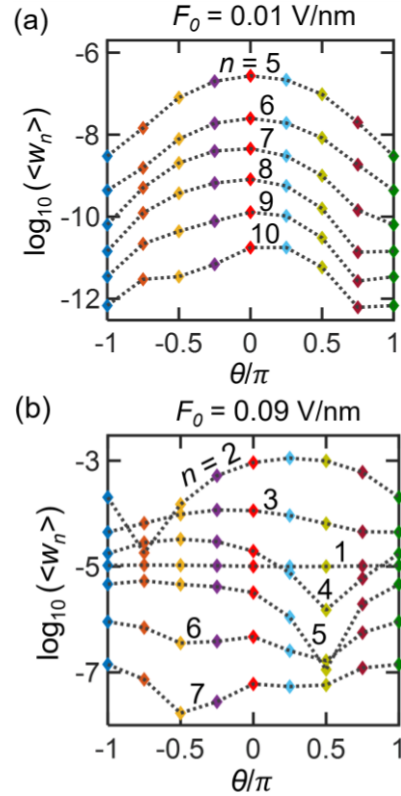
**Figure 1.** Energy diagram for electron emission under two-color laser fields and a dc bias. Electrons with initial energy of  $\varepsilon$  are emitted by absorbing photon energy  $n\hbar\omega$ , with  $n$  being an integer [8].



**Figure 2.** Photoelectron energy spectra under different in-phase (i.e.  $\theta=0$ ) laser fields and dc fields.



**Figure 3.** Emission current modulation depth  $\Gamma = (\langle w \rangle_{max} - \langle w \rangle_{min}) / (\langle w \rangle_{max} + \langle w \rangle_{min})$ . Here,  $\omega$ -laser field  $F_1$  and  $2\omega$ -laser field  $F_2$  are 1.6 and 0.22 V/nm respectively.



**Figure 4.** Time-resolved photoelectron energy spectra for the tungsten nanotip. Here, the fundamental (1560 nm) laser field  $F_1=1.8$  V/nm and the second harmonic laser field  $F_2=0.3$  V/nm.